

Formuleblad Grondmechanica

Korrels: $n = \frac{V_p}{V_g}$; $e = \frac{V_p}{V_k}$; $S = \frac{V_w}{V_p}$; $w = \frac{W_w}{W_k}$; $RD = \frac{e_{\max} - e}{e_{\max} - e_{\min}}$; $w = Se \frac{\rho_w}{\rho_k}$;

Spanning: $\sigma_{xx} = \sigma'_{xx} + p$; $\sigma_{xy} = \sigma'_{xy}$; $\sigma_0 = \frac{1}{3}(\sigma'_{xx} + \sigma'_{yy} + \sigma'_{zz})$

Stroming: $q_x = -k i_x$; $q_x = \frac{Q_x}{A_x}$; $i_x = \frac{\partial h}{\partial x}$; $h = z + \frac{p}{\gamma_w}$; $k = \frac{\kappa \gamma_w}{\mu}$; $\kappa = cd^2 \frac{n^3}{(1-n)^2}$; $i_{kr} = \frac{\gamma_n - \gamma_w}{\gamma_w}$

Falling Head Test: $h = h_0 \exp\left(-\frac{k At}{a L}\right)$; (of $k = c_v \gamma_w m_v$ voor: $\beta \rightarrow \infty$);

Put in confined aquifer: $h_0 - h = -\frac{Q}{2\pi k D} \ln\left(\frac{r}{R}\right)$; $\frac{\Delta\Phi}{\Delta s} = \frac{\Delta\Psi}{\Delta n}$ ($\Phi = kh$)

Put in unconfined aquifer: $h_0^2 - h^2 = -\frac{Q}{\pi k} \ln\left(\frac{r}{R}\right)$; $Q = \frac{n_{\text{stroombaan}}}{n_{\text{potentiaalbaan}}} k \Delta h B$

Continuüm: $\sigma_0 = K \varepsilon_{\text{vol}}$; $\tau_{xy} = 2G \varepsilon_{xy}$; $\varepsilon_{xx} = \frac{1}{E}[\sigma'_{xx} - \nu(\sigma'_{yy} + \sigma'_{zz})]$; $\frac{\sigma'_v}{\varepsilon_v} = E_{\text{oed}} = \frac{1}{m_v} = K + \frac{4}{3}G = \frac{E(1-\nu)}{(1+\nu)(1-2\nu)}$;

$K = \frac{E}{3(1-2\nu)}$; $G = \frac{E}{2(1+\nu)}$;

Koppejan: $\varepsilon = U \left[\frac{1}{C_p} + \frac{1}{C_s} \log\left(\frac{t}{t_1}\right) \right] \ln \frac{\sigma'}{\sigma'_1}$;

Bjerrum: $-\Delta e = e_1 - e = C_r \log\left(\frac{\sigma_{\text{grens}}}{\sigma_1}\right) + C_c \log\left(\frac{\sigma}{\sigma_{\text{grens}}}\right) + C_a \log\left(\frac{t}{t_1}\right)$; $\varepsilon = \frac{1}{C_{10}} \log\left(\frac{\sigma}{\sigma_1}\right)$ ($\sigma > \sigma_1$); $\varepsilon = \frac{1}{A_{10}} \log\left(\frac{\sigma}{\sigma_1}\right)$ ($\sigma < \sigma_1$);

ISO: $-\Delta e = C_c \log\left(\frac{\sigma}{\sigma_1}\right)$; $\varepsilon = \frac{-\Delta e}{1+e}$; $U = \frac{\Delta h - \Delta h_0}{\Delta h_{\infty} - \Delta h_0} = 1 - \frac{8}{\pi^2} \sum_{j=1}^{\infty} \frac{1}{(2j-1)^2} \exp[-(2j-1)^2 \frac{\pi^2 c_v t}{4h^2}]$; $U \approx \frac{2}{\sqrt{\pi}} \sqrt{\frac{c_v t}{h^2}}$ als

$U < 0.7$; $U \approx 1 - \frac{8}{\pi^2} \exp\left(-\frac{\pi^2}{4} \frac{c_v t}{h^2}\right)$ als $U > 0.5$

Consolidatie: $\frac{\partial p}{\partial t} = c_v \frac{\partial^2 p}{\partial r^2}$; $c_v = \frac{k}{\gamma_w(m_v + n\beta)}$; $\frac{c_v t}{h^2} \gg 0.1$: $\frac{p}{p_0} = \frac{4}{\pi} \cos\left[\frac{\pi}{2} \left(\frac{h-z}{h}\right)\right] \exp\left(-\frac{\pi^2 c_v t}{4h^2}\right)$; $\frac{c_v t_{99\%}}{h^2} = 1.784$;

$\frac{c_v t_{90\%}}{h^2} = 0.848$; $\frac{c_v t_{50\%}}{h^2} = 0.197$; $\frac{c_v t_{1\%}}{h^2} = 10^{-4} \frac{\pi}{4}$; $p_i(1 + \Delta t) = p_i(t) + \alpha[p_{i+1}(t) - 2p_i(t) + p_{i-1}(t)]$; $\alpha = \frac{c_v \Delta t}{(\Delta z)^2}$;

Mohr-Coulomb: $\left(\frac{\sigma'_1 - \sigma'_3}{2}\right) - \left(\frac{\sigma'_1 + \sigma'_3}{2}\right) \sin\phi - c \cos\phi = 0$; $\sin\phi = \frac{\frac{1}{2}(\sigma'_1 - \sigma'_3)}{c \cdot \cot\phi + \frac{1}{2}(\sigma'_1 + \sigma'_3)}$; $\sigma'_1 = \sigma'_3 \frac{1 + \sin\phi}{1 - \sin\phi} + 2c \frac{\cos\phi}{1 - \sin\phi}$;

Ongedraineerde sterkte: $c_u = s_u \approx \frac{\sigma'_1 - \sigma'_3}{2} = \frac{c \cos\phi + \sigma'_0 \sin\phi}{1 - \frac{1}{3} \sin\phi}$; Coulomb: $\tau_f = c + \sigma'_n \tan\delta$;

Skempton / Henkel: $\Delta p = B[\Delta\sigma_3 + A(\Delta\sigma_1 - \Delta\sigma_3)]$; $B = \frac{1}{1 + n\beta K}$; Triaxiaal: $A \approx \frac{1}{3}$ dilatant: $A < \frac{1}{3}$ contractant $A > \frac{1}{3}$;

Boussinesq: Punt: $r = 0$: $\sigma_{zz} = \frac{3}{2} \frac{P}{\pi z^2}$; Starre plaat: $z = 0$: $\frac{\sigma_{zz}}{p} = \frac{1}{2\sqrt{1-(r/a)^2}}$; $z = 0$: $u_z = \frac{\pi}{2}(1-\nu^2) \frac{\bar{p}a}{E} = \frac{\pi}{4}(1-\nu) \frac{\bar{p}a}{G}$;

Flexibele plaat: $r = 0$: $\frac{\sigma_{zz}}{p} = 1 - \frac{z^3}{(\sqrt{a^2 + z^2})^3}$; $u_z = 2(1-\nu)^2 \frac{pa}{E} = (1-\nu) \frac{pa}{G}$; Laagdikte factor: $f \approx 1 + \frac{h}{2a} - \frac{1 + \frac{1}{2}(h/a)^2}{\sqrt{1 + (h/a)^2}}$;

Flamant: Lijnlast ($r = \sqrt{x^2 + z^2}$): $\sigma_{zz} = \frac{2Fz^3}{\pi r^4}$; $\sigma_{xx} = \frac{2Fx^2z}{\pi r^4}$; $\sigma_{xz} = \frac{2Fxz^2}{\pi r^4}$; Naast gladde wand: $x = 0$: $Q_h = \frac{2}{\pi} \frac{F}{1 + (a/h)^2}$ Strip: $x = 0$: $\sigma_{zz} = \frac{2P}{\pi} \left[\arctan\left(\frac{a}{z}\right) + \frac{az}{a^2 + z^2} \right]$; $\sigma_{xx} = \frac{2P}{\pi} \left[\arctan\left(\frac{a}{z}\right) - \frac{az}{a^2 + z^2} \right]$;

Naast gladde wand: $Q_h = \frac{2}{\pi} ph \arctan\left(\frac{a}{h}\right)$;

Horizontaaldruk: $K_e = \frac{\nu}{1-\nu}$; $K_0 \approx 1 - \sin\phi$; $K_a = \frac{1 - \sin\phi}{1 + \sin\phi}$; $K_p = \frac{1 + \sin\phi}{1 - \sin\phi}$; $\sigma'_{h-\min} = K_a \sigma'_v - 2c\sqrt{K_a}$; $\sigma'_{h-\max} = K_p \sigma'_v + 2c\sqrt{K_p}$; $Q = \frac{1}{2} K \gamma h^2$; $Q_h = Q \sin(\alpha - \delta)$

Strookfundering: Prandtl: ($\phi = 0$): $p_c = (\pi + 2)c$; Brinch Hansen: $p_c = cN_c i_c s_c + qN_q i_q s_q + \frac{1}{2} \gamma B N_{\gamma} i_{\gamma} s_{\gamma}$; $N_q = \frac{1 + \sin\phi}{1 - \sin\phi} \exp(\pi \tan\phi)$; $N_c = (N_q - 1) \cot\phi$; $N_{\gamma} = 2(N_q - 1) \tan\phi$;

$i_c = 1 - \frac{t}{c + p \tan\phi}$; $i_q = i_c^2$; $i_{\gamma} = i_c^3$; $s_c = 1 + 0.2 \frac{B}{L}$; $s_q = 1 + \frac{B}{L} \sin\phi$; $s_{\gamma} = 1 - 0.3 \frac{B}{L}$ ($L \geq B$)

Oneindig talud: ($c = 0$): $F \approx \frac{\tan\phi}{\tan\alpha}$; Stroming evenwijdig oppervlak: $F \approx \frac{\gamma_n - \gamma_w}{\gamma_n} \frac{\tan\phi}{\tan\alpha}$; Horizontale stroming: $F \approx \frac{\gamma_n - (\gamma_w / \cos^2 \alpha) \tan\phi}{\gamma_n \tan\alpha}$

Eindig talud: Fellenius: $F \approx \frac{\sum [(c + (\gamma h \cos^2 \alpha - p) \tan\phi) / \cos\alpha]}{\sum \gamma h \sin\alpha}$; Bishop: $F \approx \frac{\sum \frac{c + (\gamma h - p) \tan\phi}{\cos\alpha(1 + \tan\alpha \tan\phi / F)}}{\sum \gamma h \sin\alpha}$

